

An  $n$ -distinguishing coloring of a graph  $G$ , with vertex set  $V_G$ , is a map  $\phi : V_G \rightarrow \{1, 2, \dots, n\}$  such that, for any nontrivial automorphism  $f$  of  $G$ ,  $\phi(v) \neq \phi(f(v))$  for every  $v \in V_G$ . The distinguishing number of a graph  $G$ , denoted  $D(G)$ , is the smallest number  $n$  such that  $G$  has an  $n$ -distinguishing coloring.

This talk will cover several aspects of distinguishing colorings, and compare the distinguishing number of a graph to other, more familiar, properties of the graph, including the maximum degree of a vertex, and the chromatic number. In addition, we will look at colorings which are both distinguishing and proper, as well as consider a generalization of this concept to arbitrary group actions on sets.